Aim: How can we determine differentiability?

Get Ready: Please determine if the function is continuous. If not, state the domain where the function is not continuous.

$$f(x) = \begin{cases} 3x + 2, x \le -2 \\ x^2 - 8, x > -2 \end{cases}$$
2. $g(x) = \sqrt{x^2 + 2x - 8}$

3.
$$g(x) = \sqrt[5]{3x-5}$$
 4. $h(x) = \frac{x+2}{x^2-x-6}$

$$f(x) = \begin{cases} 2x^2 - 4, x > 3\\ 3x + 4, x \le 3 \end{cases}$$

6. Find "a" that makes f(x) continuous $f(x) = \begin{cases} a^2x^2 + 3x + 2, x < 1 \\ -3ax + 9, x \ge 1 \end{cases}$

I. Differentiability:

Differentiability At a Point: Function f(x) is differentiable at x=c if f'(c) exists. (f'(c)) = real number

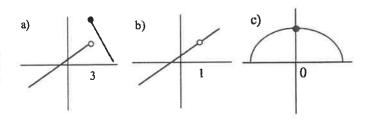
Differentiability On An Interval: Function f(x) is differentiable on an interval (a,b) if and only if it is differentiable for every value of x on the interval (a,b).

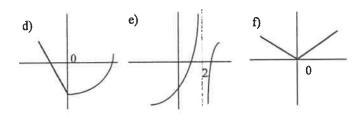
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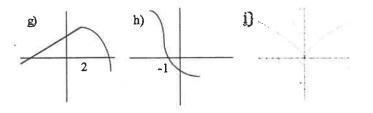
II. Differentiability→"Smooth" A

differentiable curve will have no sharp points (cusps or corners) or vertical tangent lines. A curve must be continuous at all points. Differentiability implies continuity. Continuity does not imply differentiability.

III. Determine whether the following functions are continuous, differentiable, or both.







Aim: How can we determine differentiability? IV. Determine whether the functions are differentiable.

a.
$$f(x) = x^2 - 6x + 1$$

$$f(x) = \frac{x^2 - x - 12}{x + 3}$$

c.
$$f(x) = \sin x$$

$$f(x) = \frac{\sin x}{x}$$

V. Determine if the function if differentiability at the point where the rule(curve) changes.

$$f(x) = \begin{cases} 4 - x, x < 2 \\ x^2 - 6x + 10, x \ge 2 \end{cases}$$

$$f(x) = \begin{cases} -x - 4, x < -1 \\ x^2 + x - 3, x \ge -1 \end{cases}$$
b.

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$$f(x) = \frac{x^2 - x - 12}{x + 3}$$
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$$f(x) = \begin{cases} 4 - \sqrt[3]{x - 4}, & x < 4 \\ \sqrt{x + 5}, & x \ge 4 \end{cases}$$

$$f(x) = \begin{cases} \sin x, x \ge 0 \\ x - 3x^2, x < 0 \end{cases}$$

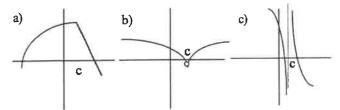
VI. Find the values of "a" and "b" that make f(x) differentiable.

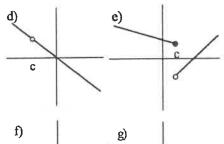
$$f(x) = \begin{cases} ax^2 + 1, x \ge 1 \\ bx - 3, x < 1 \end{cases}$$

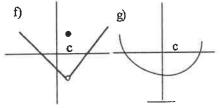
$$f(x) = \begin{cases} ax^3 + 1, x < 2 \\ b(x-3)^2 + 10, x \ge 2 \end{cases}$$
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VII. Mixed Practice

1. Determine whether the following functions are continuous, differentiable, both, or neither at .=c.







2. Determine whether the following functions are continuous, differentiable, both, or neither. Show necessary work.

$$f(x) = \begin{cases} x^2, x \ge 0 \\ x, x < 0 \end{cases}$$

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$$f(x) = \begin{cases} x^2 + x - 7, x \ge 2\\ 5x - 11, x < 2 \end{cases}$$

$$f(x) = \begin{cases} \sqrt{x} - 3, x > 1 \\ \frac{1}{2}x - \frac{5}{2}, x \le 1 \end{cases}$$
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$$f(x) = \begin{cases} \sin(x), x > 0 \\ x, x \le 0 \end{cases}$$

$$f(x) = \begin{cases} \cos(x), x \ge 0 \\ 1 - x^2, x < 0 \end{cases}$$

$$f(x) = \begin{cases} 3 + (x+2)^{\frac{1}{3}}, x \ge -2\\ 3 - (x+2)^{\frac{2}{3}}, x < -2 \end{cases}$$

3. Find the values of "a" and "b" that make the function differentiable.

$$f(x) = \begin{cases} x^3, x \ge 1 \\ a(x-2)^2 + b, x < 1 \end{cases}$$

$$f(x) = \begin{cases} ax^2 + 10, x \ge 2\\ x^2 - 6x + b, x < 2 \end{cases}$$

$$f(x) = \begin{cases} \frac{a}{x}, x \ge 1\\ 12 - bx^2, x < 1 \end{cases}$$

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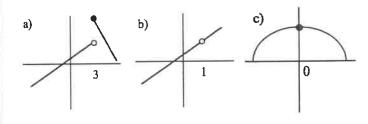
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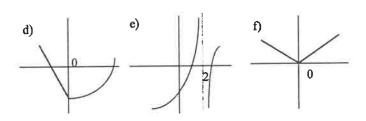
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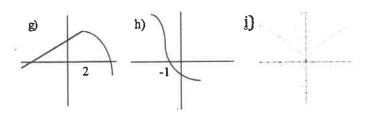
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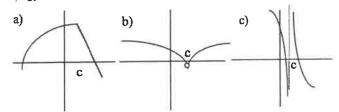
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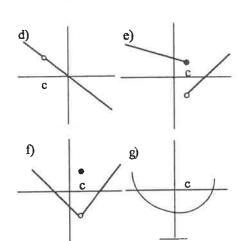
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